

# ddpcRquant

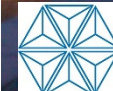
Wim Trypsteen

Summer Course HIV quantification  
21-25 september 2015, Ghent

Sponsored by:



GILEAD



Bristol-Myers Squibb

## Normality & Extreme Value Theory

ddpcRquant overview

Input & Automation

NTC Pre-Processing

NTC Processing

Sample Processing

Output

Take Home Messages

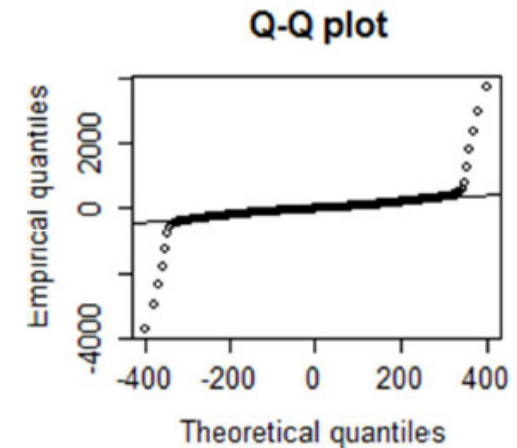
## 135 NTCs: Anderson Darling test

The hypotheses for the Anderson-Darling test are:

H0: The data follows a specified distribution

H1: The data does not follow a specified distribution

$P < 0.05$ : reject H0



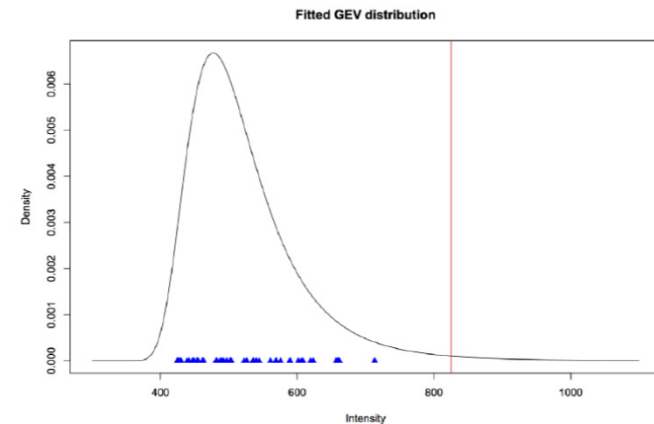
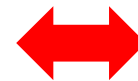
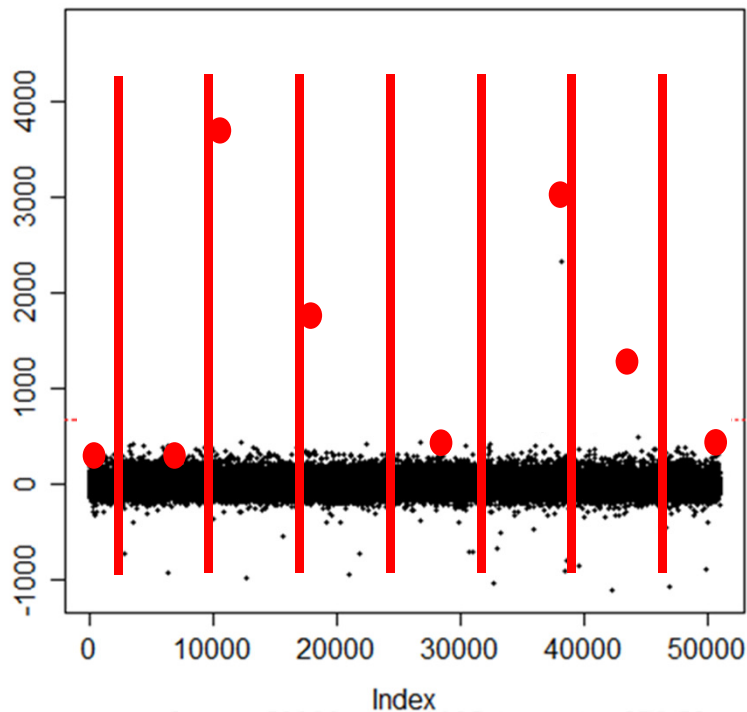
- 128 Not likely to follow normal distribution ( $p < 0.000001$ )
- 2 Not likely to follow normal distribution ( $0.05 > p > 0.001$ )
- 5 Likely to follow normal distribution ( $p > 0.05$ )

**Tails => other distributions?  
extreme value theory**

**Fisher-Tippett theorem:** The distribution of block maxima is given by the Generalized Extreme Value distribution (GEV) and no other!

= **Block maxima (extremes) follow the same distribution**

merged\_ntc\_threshold\_RU5.png





**Fisher-Tippett theorem:** The distribution of block maxima is given by the Generalized Extreme Value distribution (GEV) and no other!

**Block:** subsample of the datapoints

**Block maxima:** extreme values (per block droplet with highest fluorescence)

**GEV model:** Fits 3 parameters (location, scale and shape) to build the distribution model

**Block size:** number of droplets per block

- Needs to be large enough for the Fisher-Tippett theorem to hold
- Important factor to optimize (too small, too large (bad model))

Normality & Extreme Value Theory

## **ddpcRquant overview**

Input & Automation

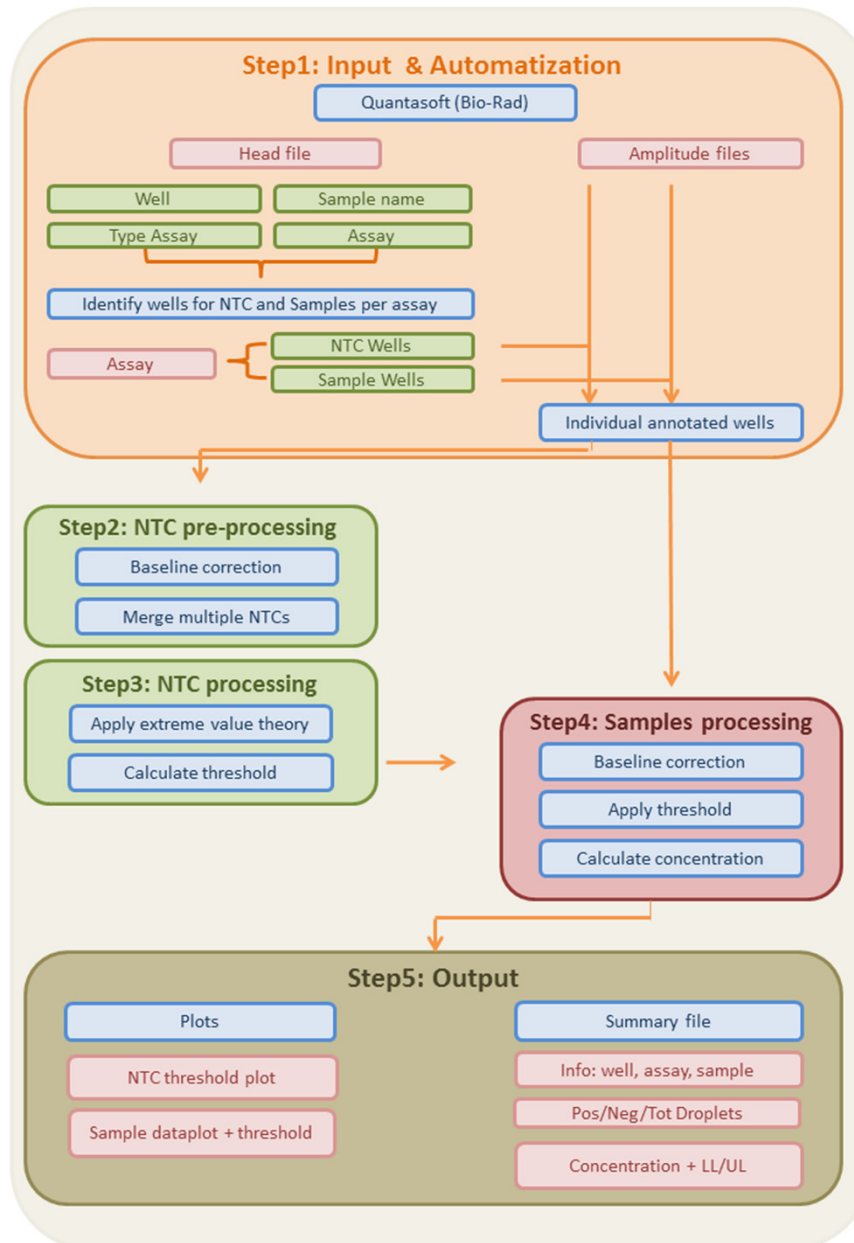
NTC Pre-Processing

NTC Processing (Treshold calculation)

Sample Processing

Output

Take Home Messages



1-D data = 1 channel at a time

Set single threshold based on NTC negative droplet population

Normality & Extreme Value Theory

## **ddpcRquant overview**

### **Input & Automation**

NTC Pre-Processing

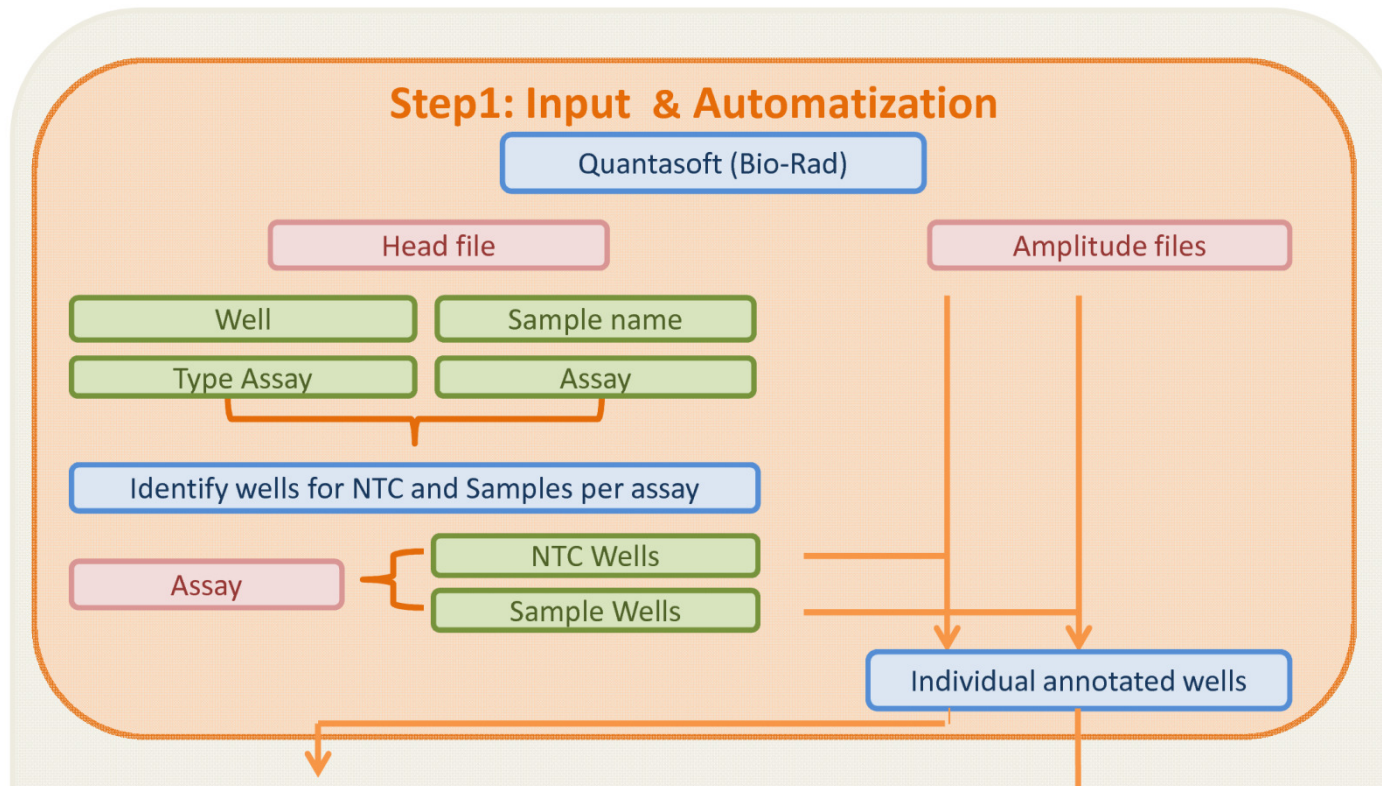
NTC Processing

Sample Processing

Output

Take Home Messages





**Goal:** Annotate individual wells with sample & assay info  
Retrieve Fluorescence Data per sample

*See hands-on for details*

Normality & Extreme Value Theory

## **ddpcRquant overview**

Input & Automation

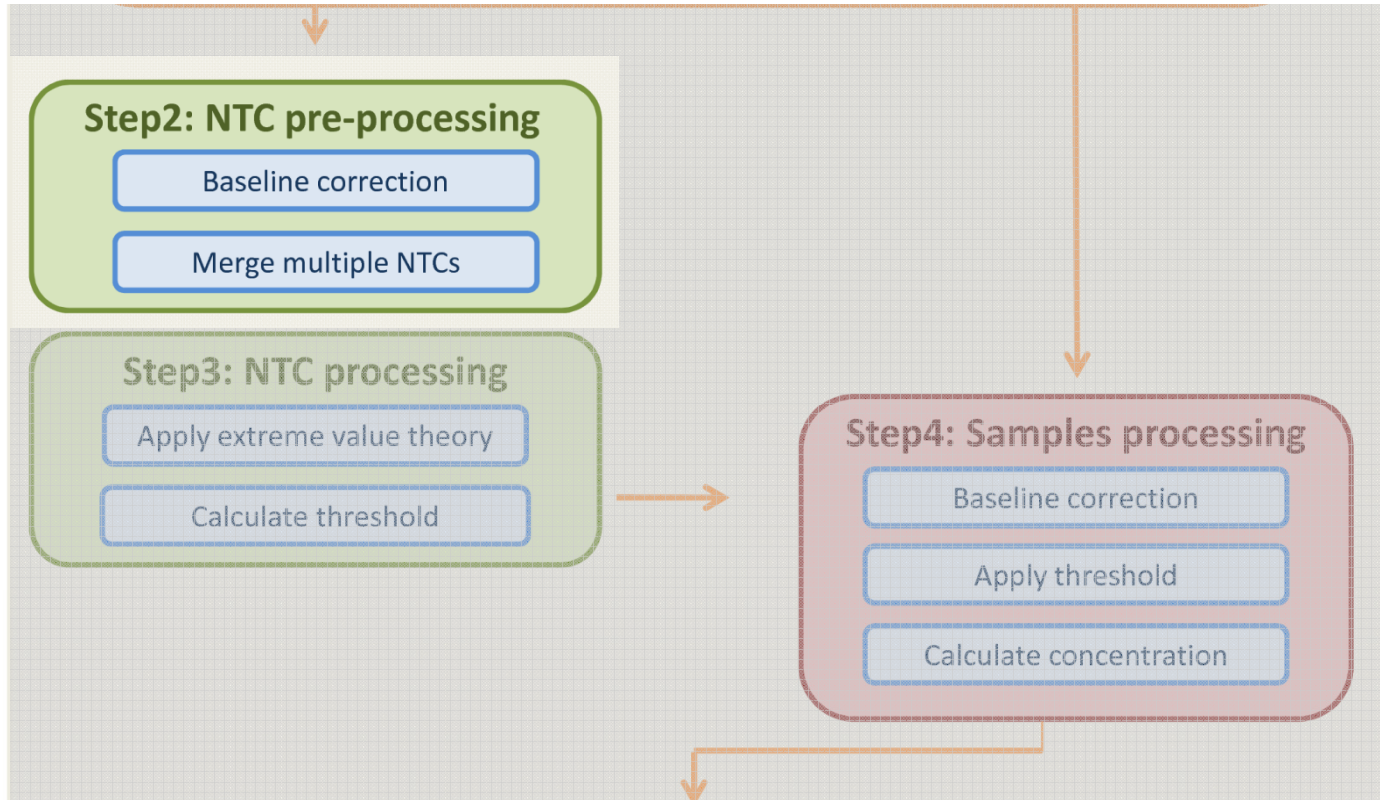
### **NTC Pre-Processing**

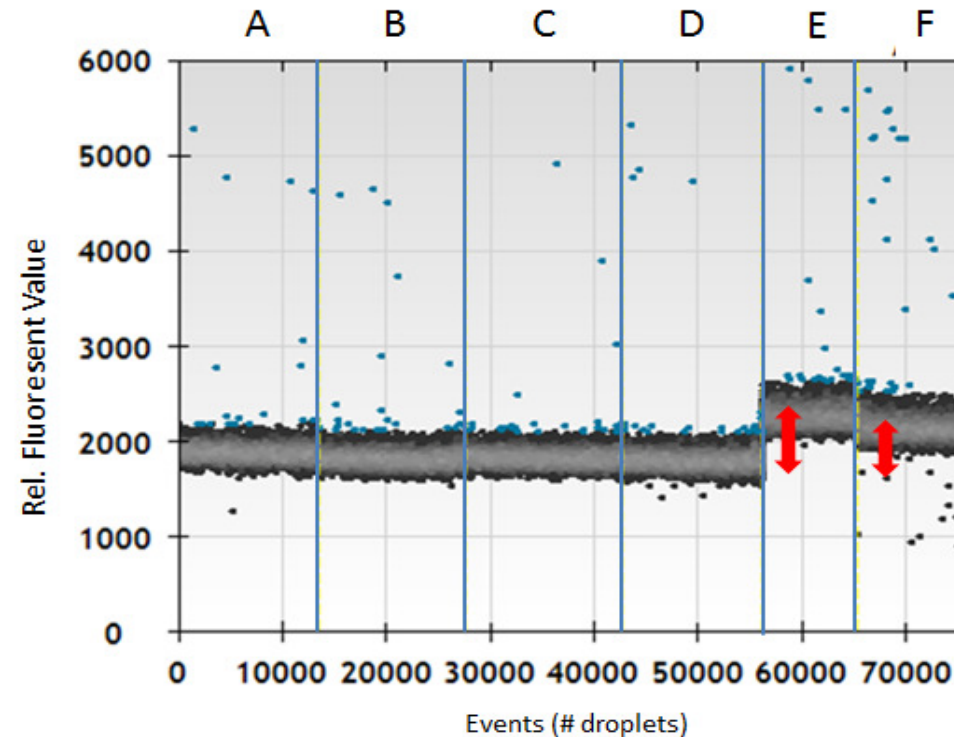
NTC Processing

Sample Processing

Output

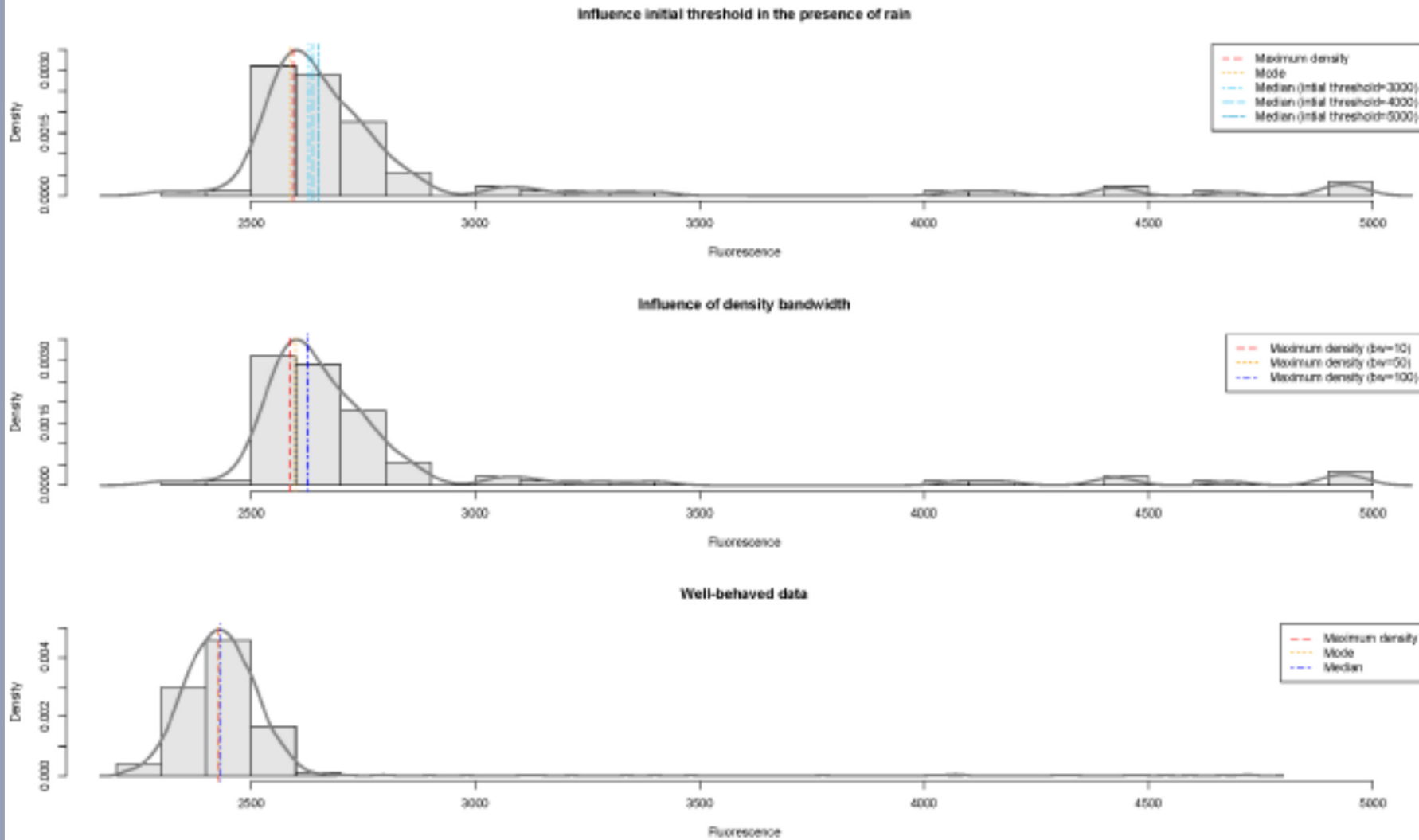
Take Home Messages

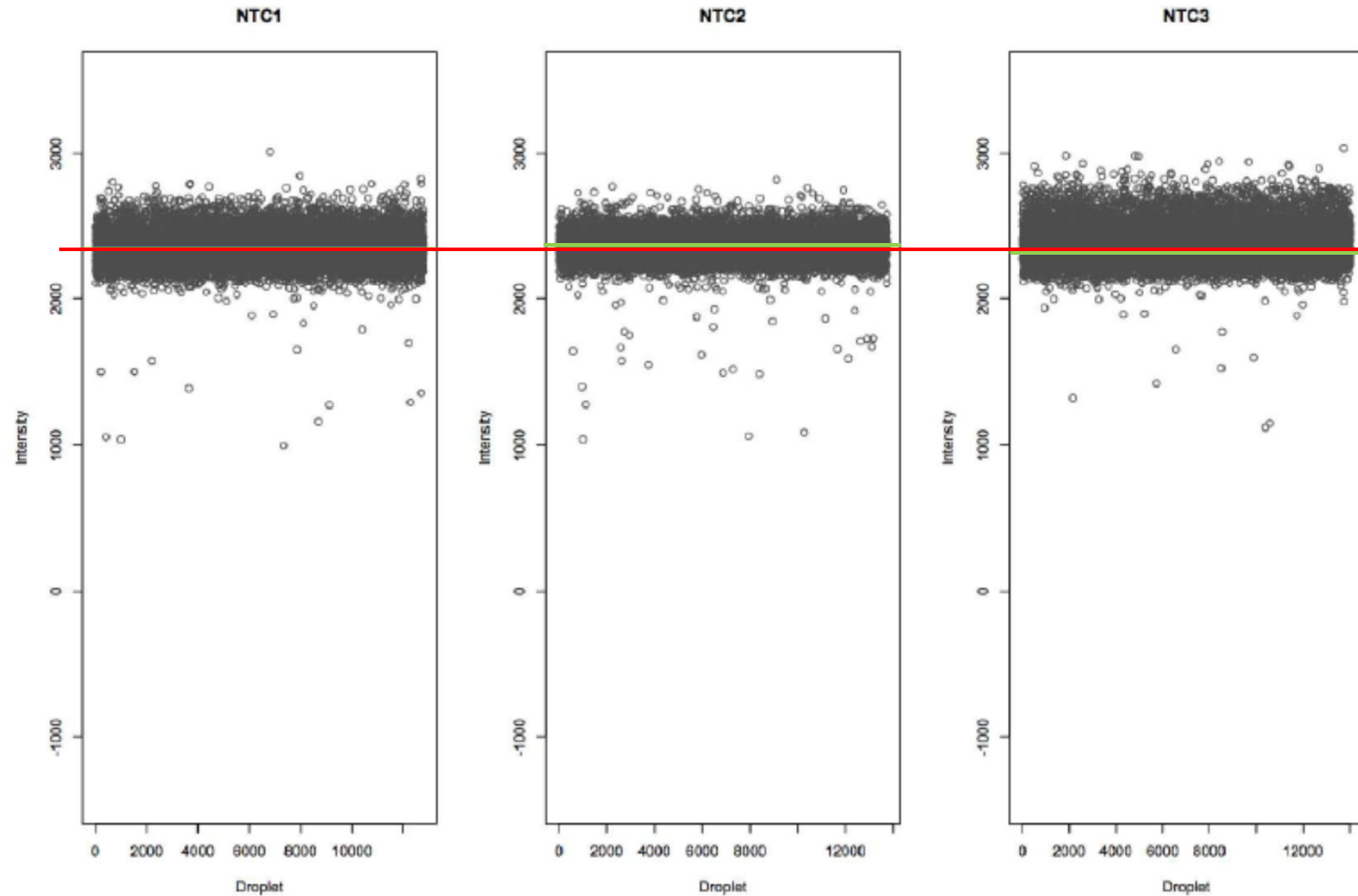




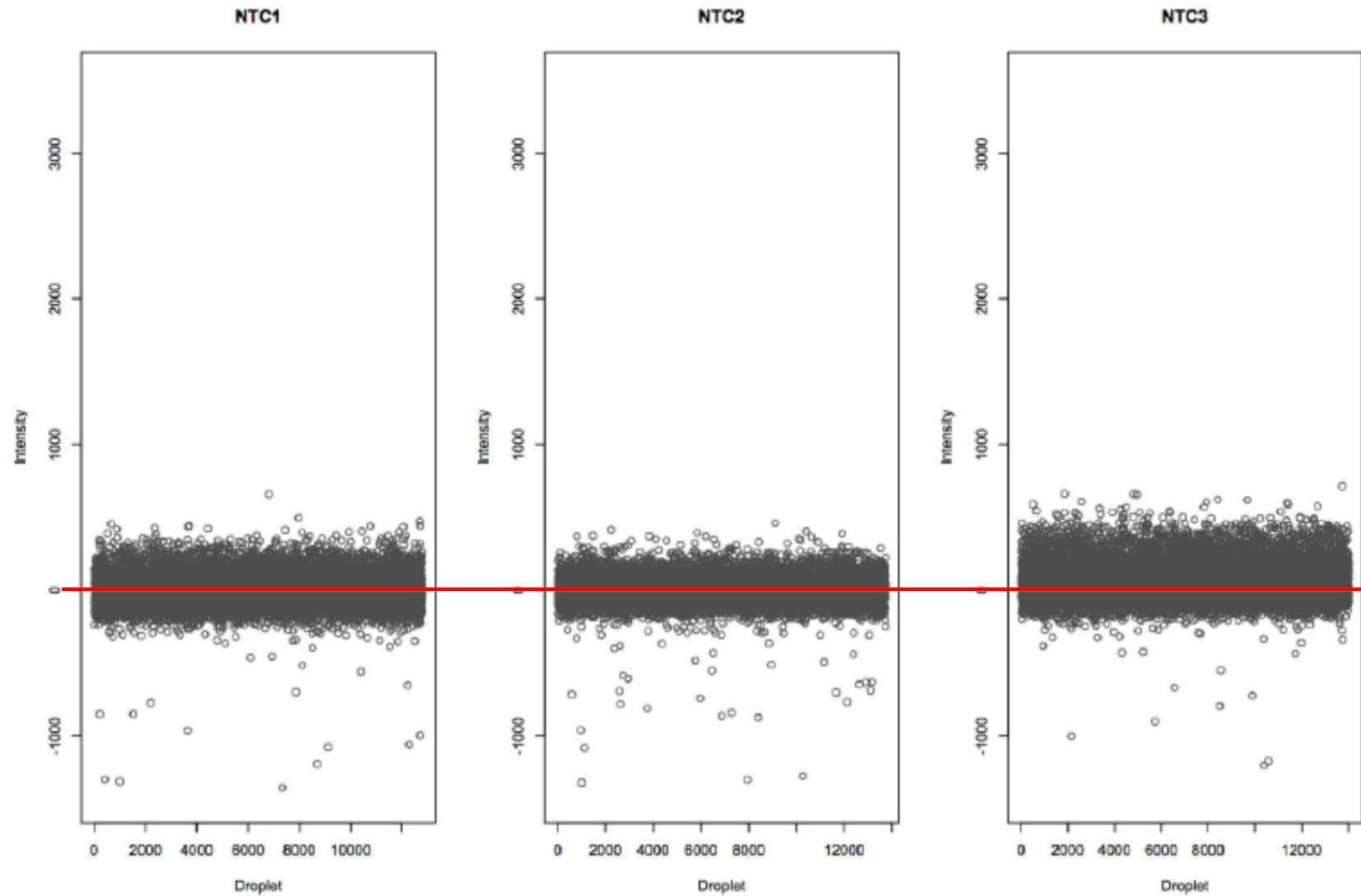
## Baseline correction (shift) + merge (increase datapoints)

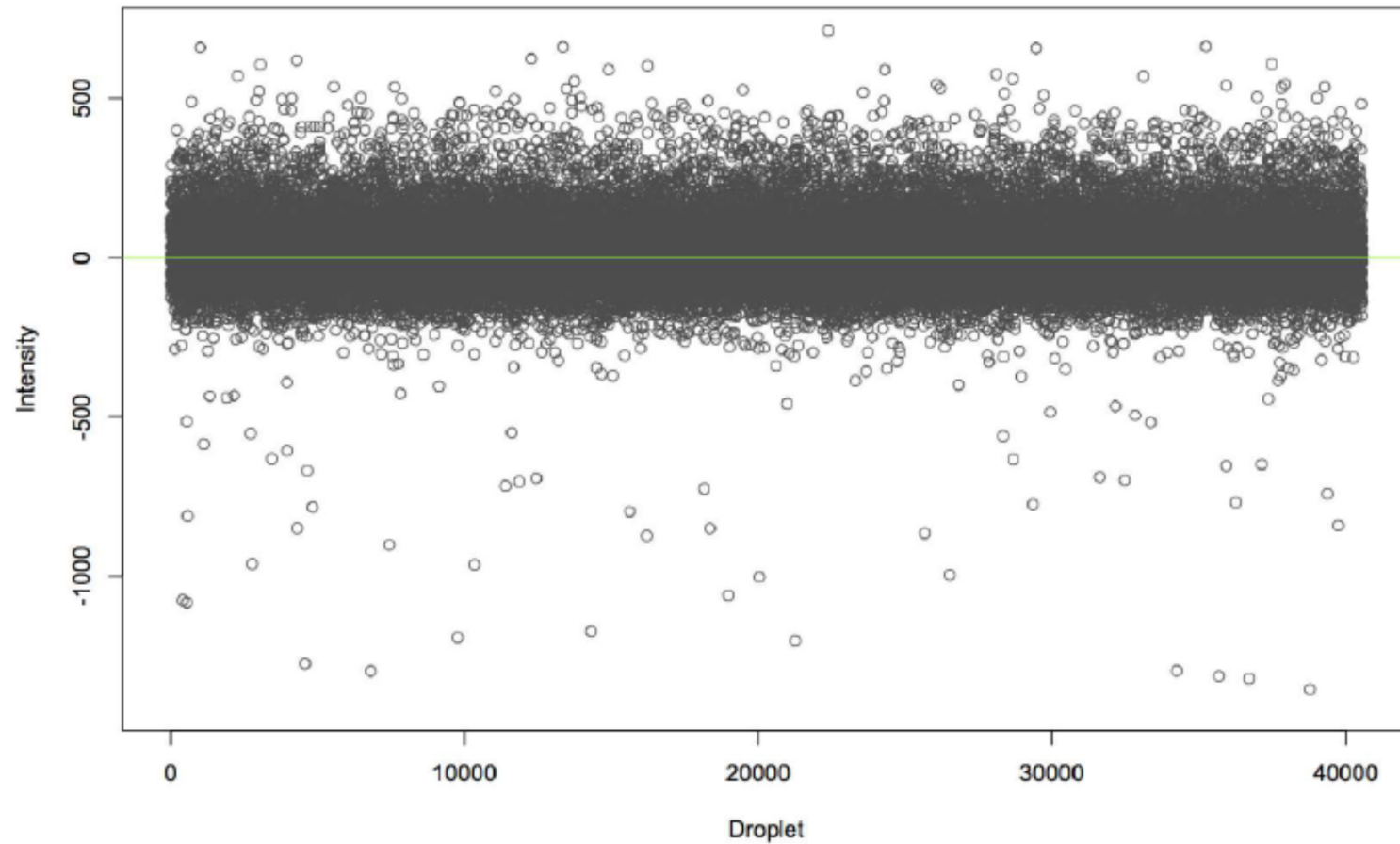
- Find a value to subtract from all droplets
- Evaluation of median, maximum density and mode











Normality & Extreme Value Theory

## **ddpcRquant overview**

Input & Automation

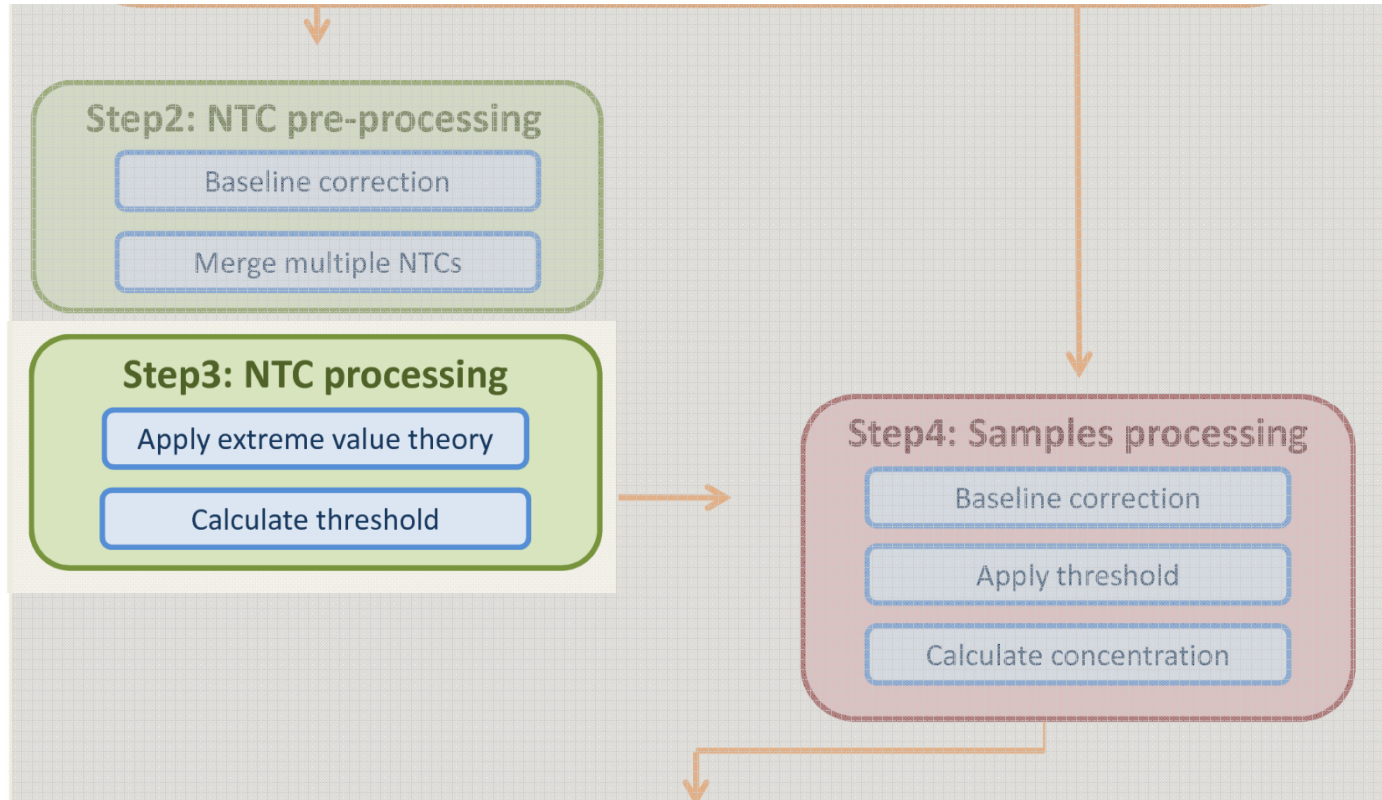
NTC Pre-Processing

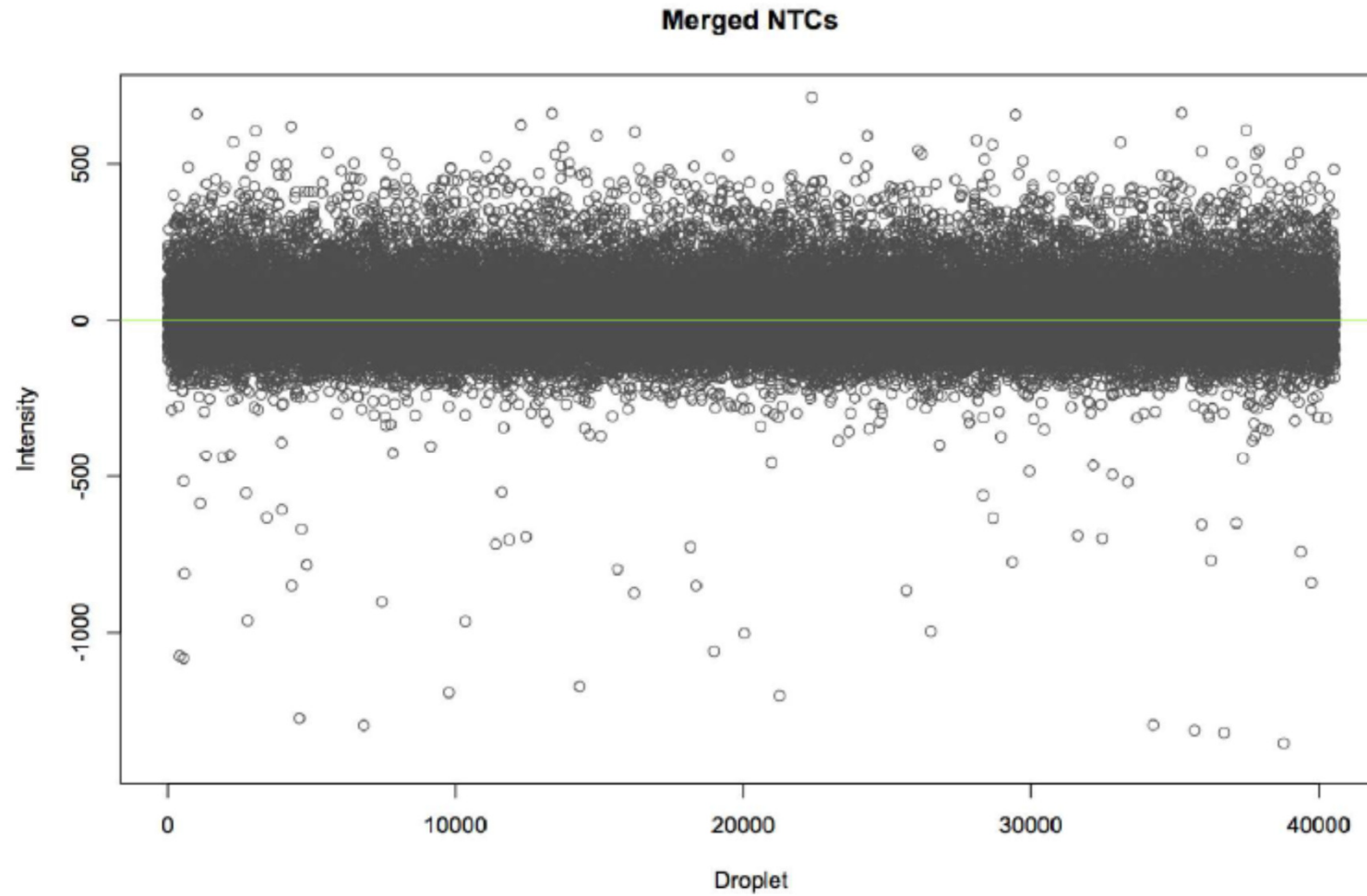
## **NTC Processing**

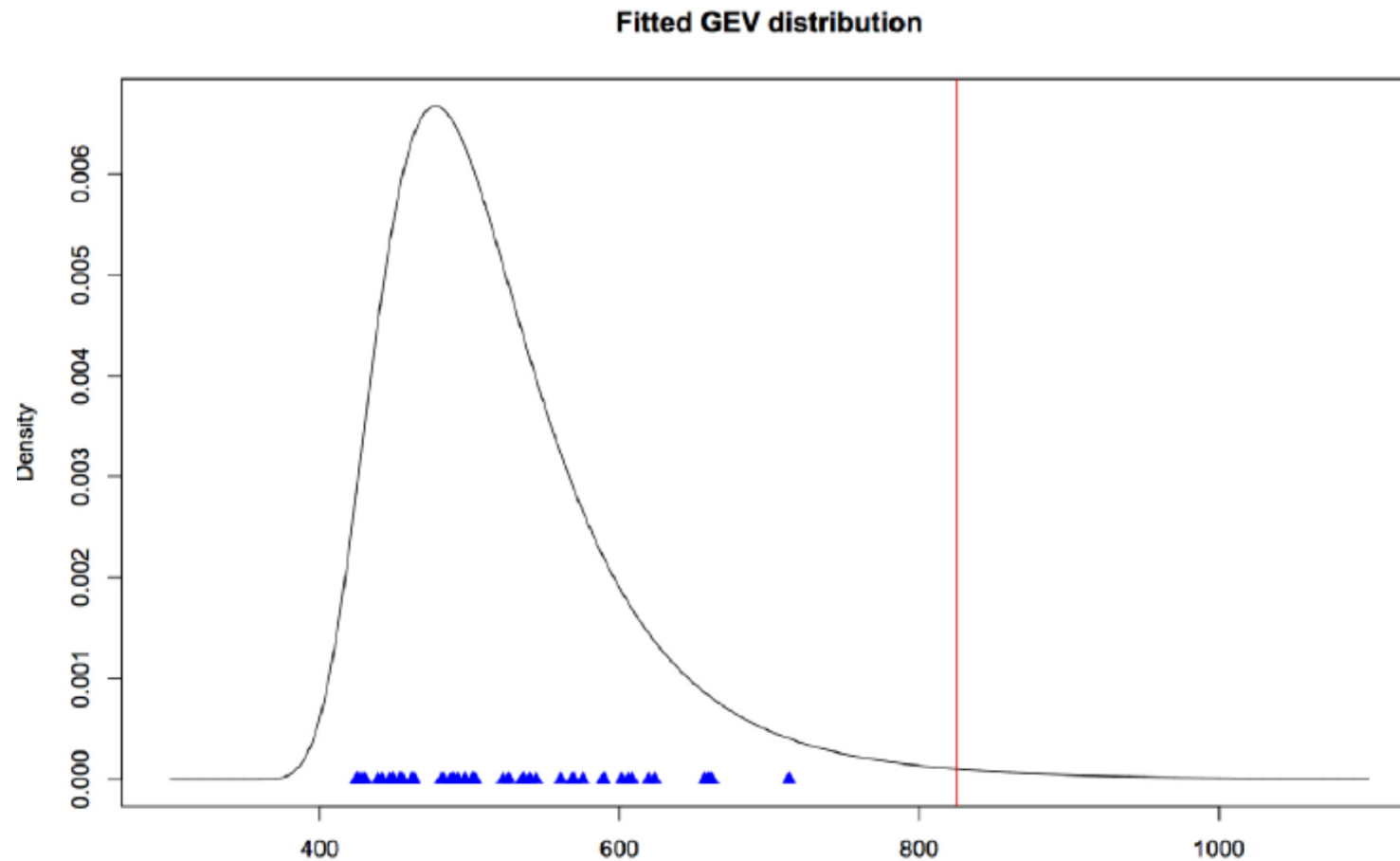
Sample Processing

Output

Take Home Messages







**GEV( $\mu$ ,  $\sigma$ ,  $\xi$ )**

$$\frac{1}{\sigma} t(x)^{\xi+1} e^{-t(x)},$$

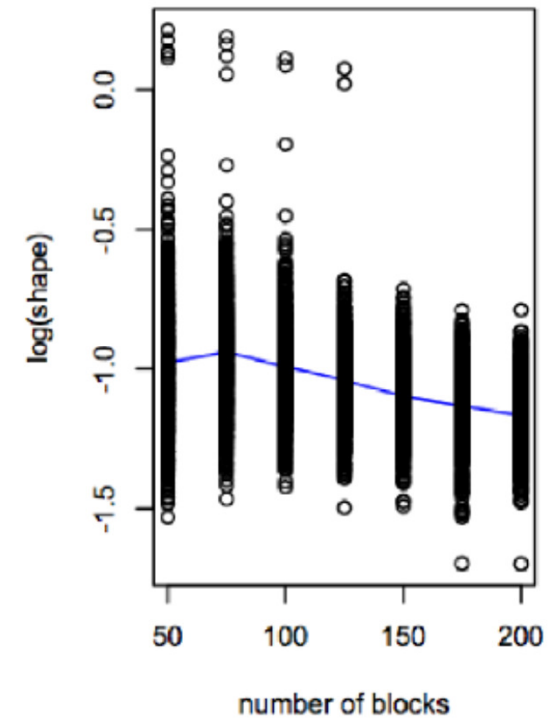
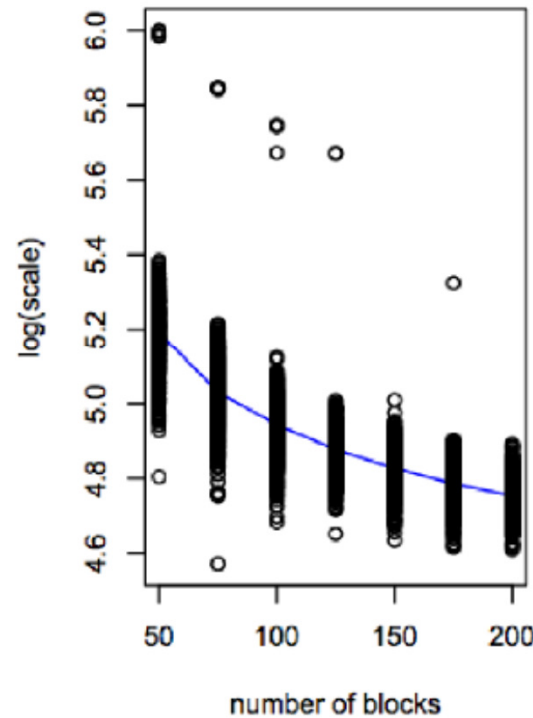
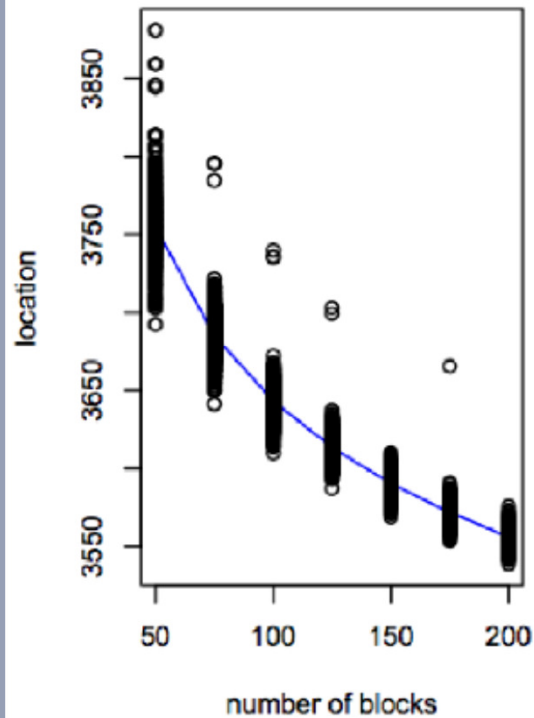
where

$$t(x) = \begin{cases} \left(1 + \left(\frac{x-\mu}{\sigma}\right)\xi\right)^{-1/\xi} & \text{if } \xi \neq 0 \\ e^{-(x-\mu)/\sigma} & \text{if } \xi = 0 \end{cases}$$

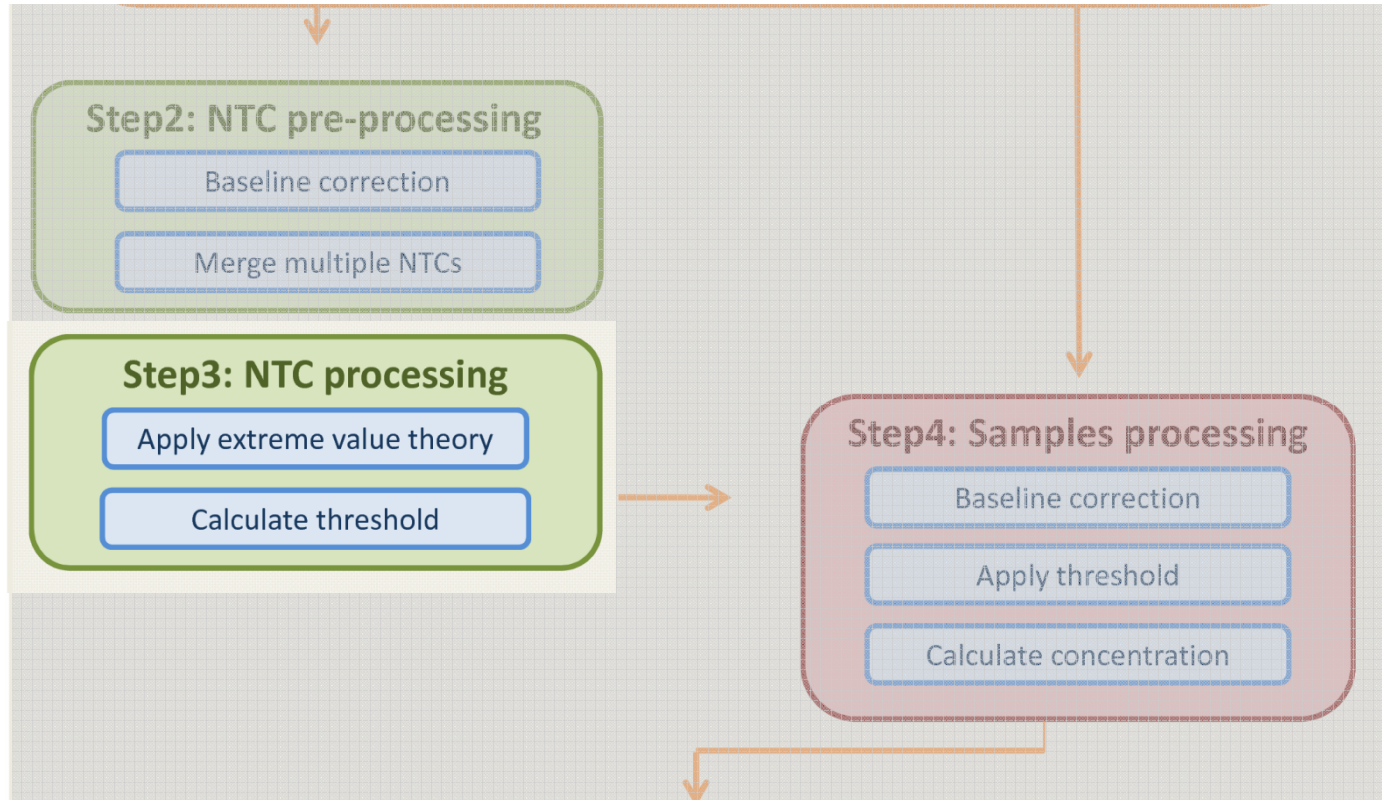
This function takes 3 parameters: location, scale and shape to be modelled based on the extremes

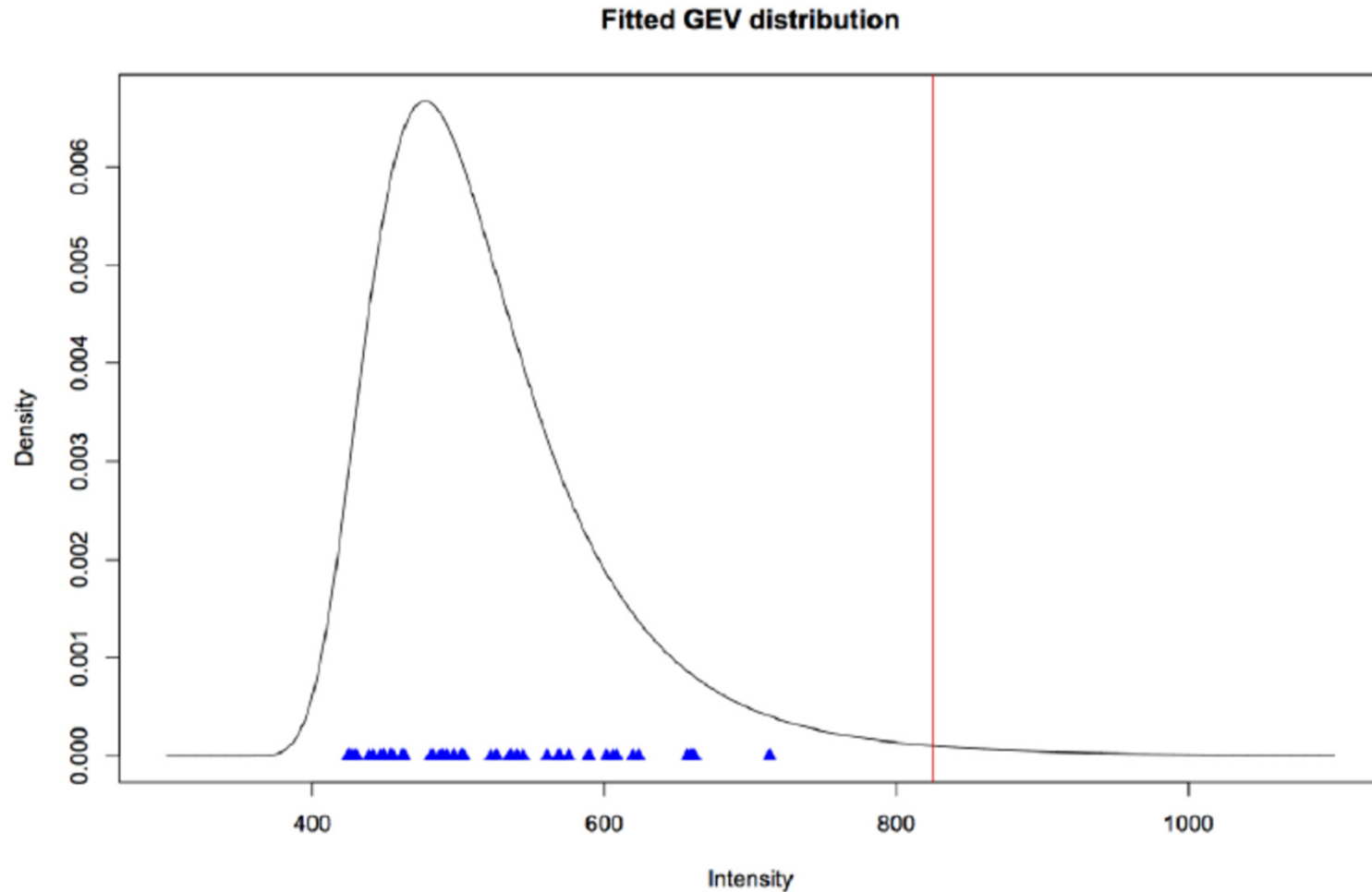


**3 parameters to be determined: location / scale / shape (block size!)**

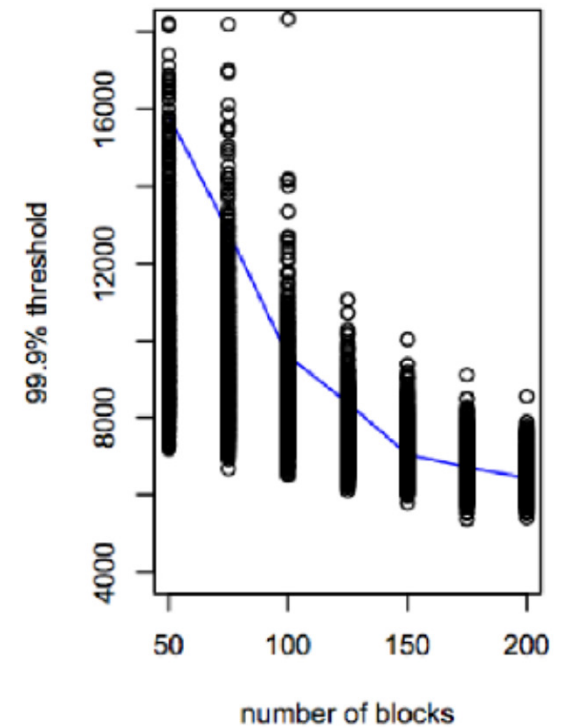
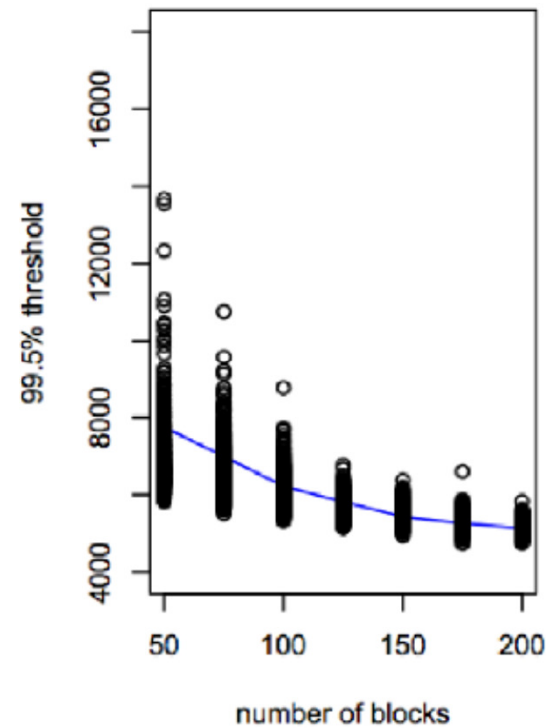
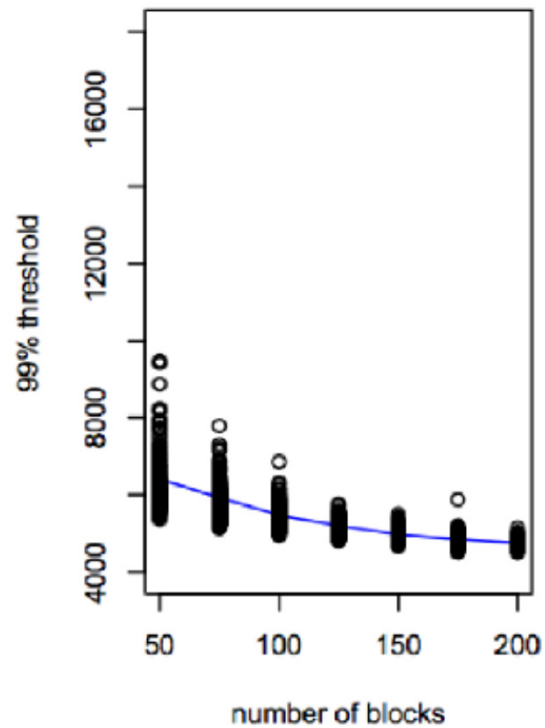


**Block number too small** variation bigger  
**Block number too big** not anymore looking at extreme values  
 fisher tippet theorem does not hold





**Threshold** percentile of the modelled GEV distribution  
 depends on block size + user defined percentile



**Increase in number of blocks lowers threshold variation**  
**Increase in threshold value with increased percentile**

## Threshold rules of thumb

We advise to scale up the blocks with the number of NTCs you have run to have the optimal threshold calculation (standard in `ddpcRquant`)  
=> fisher-tippett theorem + variation increases

We evaluated calculated threshold levels and determined a default value of 99.95 % (but is user defined!)

## Threshold interpretation

Based on the extremes of the NTC you can say that if you go above the threshold (0.9999) you have 1 in 10000 chance that the extreme event in the sample is a false positive

Normality & Extreme Value Theory

## **ddpcRquant overview**

Input & Automation

NTC Pre-Processing

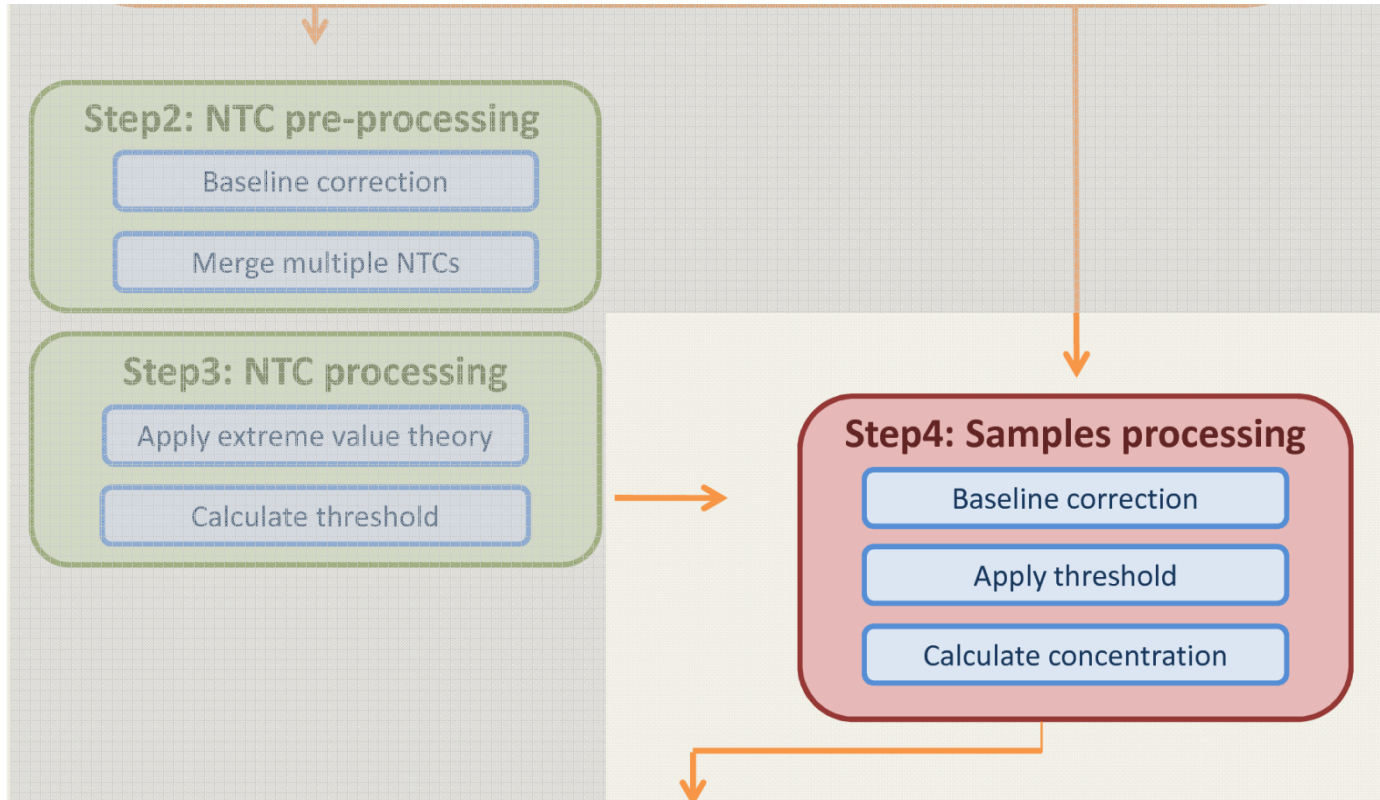
NTC Processing

## **Sample Processing**

Output

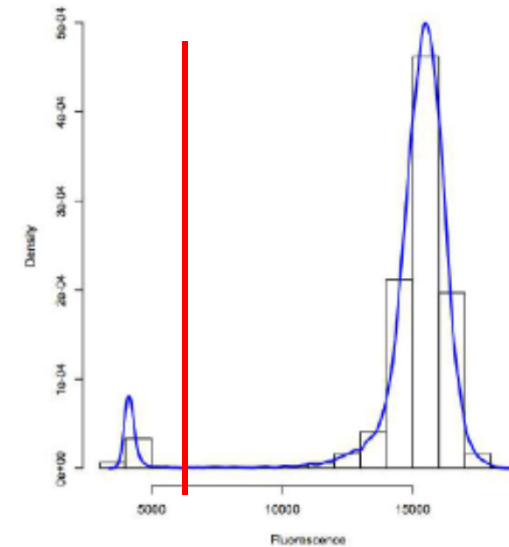
Take Home Messages





## 1. Determine the mode (cfr. NTC)

- Difficulty: multiple droplet populations
- We need starting value for mode estimation
- Automated:  $\text{mean}(\text{NTC modes}) + \text{threshold}$

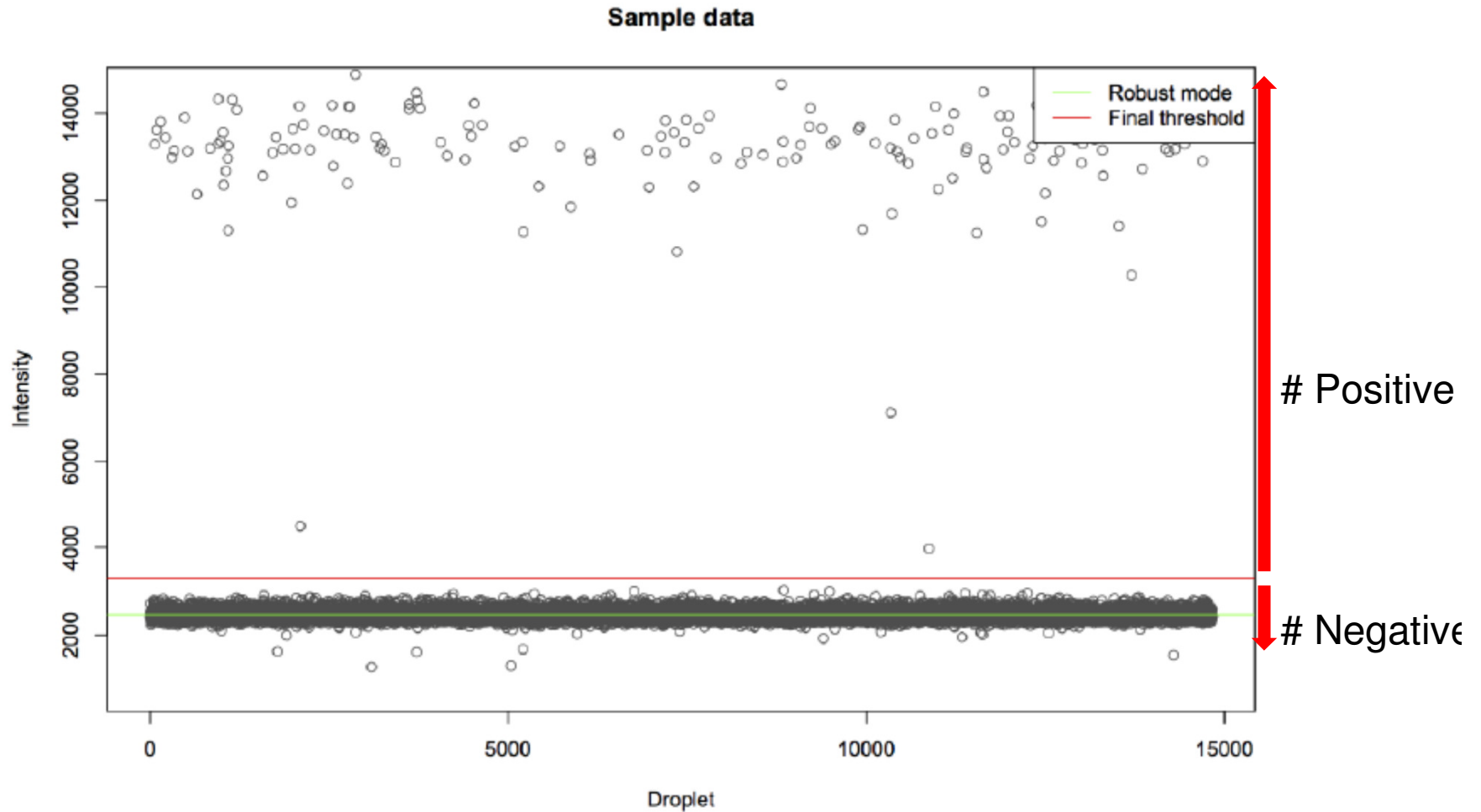


**Important:** Run NTCs with template free gDNA (background fluo)

## 2. Apply threshold

Sample Threshold = Calculated Sample Mode + Threshold value

## 3. Quantification by Poisson distribution calculations



$$C = -\ln\left(\frac{N_{neg}}{N}\right) * \frac{1000}{Vd} * D$$

Normality & Extreme Value Theory

## **ddpcRquant overview**

Input & Automation

NTC Pre-Processing

NTC Processing

Sample Processing

## **Output**

Take Home Messages



## Step5: Output

Plots

NTC threshold plot

Sample dataplot + threshold

Summary file

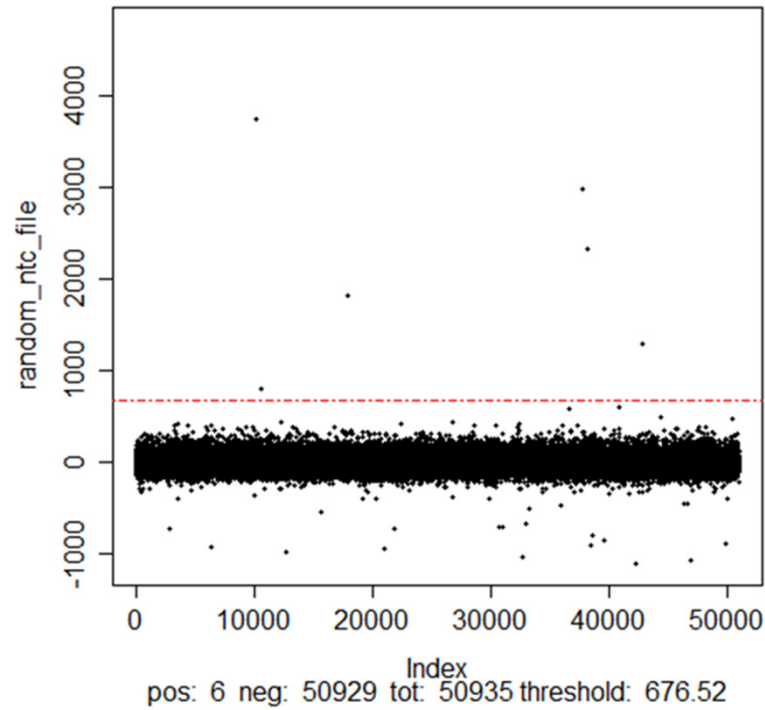
Info: well, assay, sample

Pos/Neg/Tot Droplets

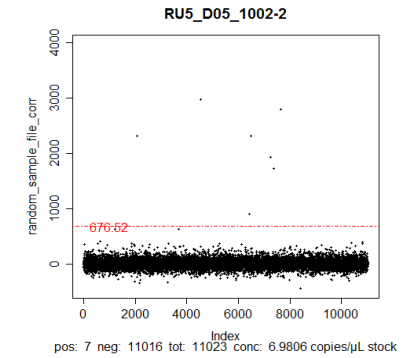
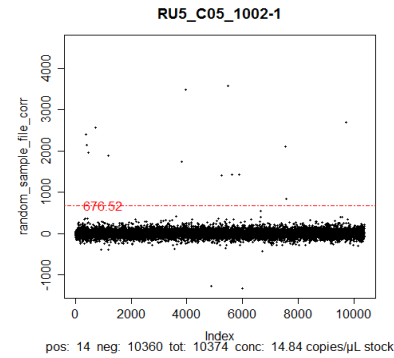
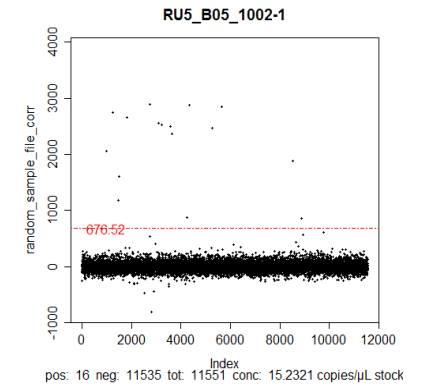
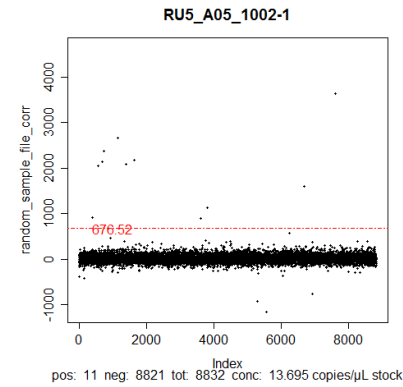
Concentration + LL/UL

## MERGED NTC + threshold

merged\_ntc\_threshold\_RU5.png



## SAMPLES





## Csv file

Well	assay	name	type	positive droplets	negative droplets	total droplets	concentration	lowerCI	upperCI
1 merged	2 LTR	merged_NTC	ntc	1	19376	19377	0.5671	0.0666	4.8298
2 E01	2 LTR	gDNA 1	sample	116	10957	11073	115.7274	91.1503	146.887
3 F01	2 LTR	gDNA2	sample	163	10391	10554	171.0427	139.8199	209.1717
4 G01	2 LTR	plas 1	sample	1	12425	12426	0.8844	0.1038	7.531
5 H01	2 LTR	plas 2	sample	9	7758	7767	12.7409	5.5316	29.3334

HTML file: <http://www.ddpcrquant.ugent.be/output/RnaseP.html>

Normality & Extreme Value Theory

## **ddpcRquant overview**

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## **Take Home Messages**

**Extremes follow GEV distribution and no other (Fisher-Tippett)**

**Block size has an effect on the parameter estimation of the GEV**

**Threshold = percentile of the GEV model based on the extremes  
(data points)**